## University Physics 226N/231N Old Dominion University

# **More on Circular Motion**

First "Midterm" is Wednesday, September 19! Today's quiz is 2 problems on MasteringPhysics starting around 9:20

Hardcopies are also available if you want to work on paper

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Friday, September 14 2012

Happy Birthday to Amy Winehouse, Wendy Thomas (Wendy's) and Walter Koenig (Chekhov)! Happy Cream-Filled Donut day, Feast of the Cross, and Eat a Hoagie Day.

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## **Uniform Circular Motion**

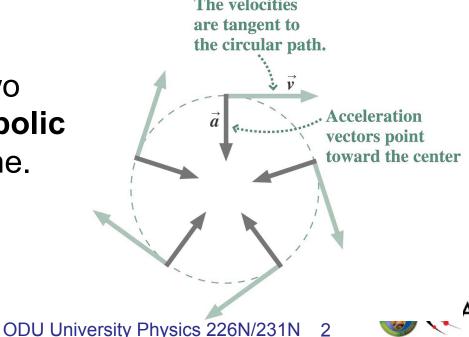
 When an object moves in a circular path of radius r at constant speed v, its acceleration has magnitude

$$a = \frac{v^2}{r}$$

- The acceleration vector points toward the center of the circle.
- Since the direction of the acceleration keeps changing, this is not constant acceleration.
  The velocities
- Constant acceleration in two dimensions implies a parabolic trajectory, not a circular one.

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## **Nonuniform Circular Motion**

- In nonuniform circular motion, speed and path radius can both change.
- The acceleration has both radial and tangential components, and these here also make a right triangle in those coordinates:

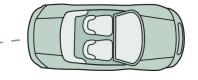
$$\vec{a} = \vec{a}_r + \vec{a_t}$$

$$a = \sqrt{a_r^2 + a_t^2}$$

- $\vec{a}_r$  is perpendicular to  $\vec{v}$ while  $\vec{a}_t$  is tangential to  $\vec{v}$ .
  - The figure shows a car
    braking as it rounds a curve.

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The car is slowing, so its tangential acceleration  $\vec{a}_t$ is opposite its velocity.



The radial acceleration  $\vec{a}_r$  changes only the direction of motion.

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## Summary

- In two and three dimensions, position, velocity, and acceleration become vector quantities.
  - Velocity is the rate of change of position:  $\stackrel{\mathbf{r}}{v} = \frac{d\hat{r}}{dt}$
  - Acceleration is the rate of change of velocity:  $\stackrel{\mathbf{r}}{a}$  =
- In general, acceleration changes both the magnitude and direction of the velocity.
- Projectile motion results from the acceleration of gravity.

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In uniform circular motion, the \_\_\_\_\_
 acceleration has magnitude v<sup>2</sup>/r and points toward the center of the circular

80

60-

100 150 200 250 300

*x* (m)

 $\Delta \vec{v} = \vec{a} \Delta t$ 

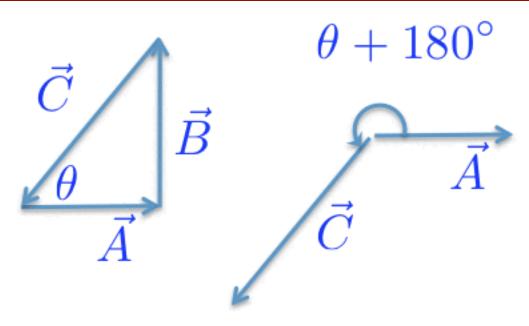
dv

dt

 $\vec{v}_0$ 

 $\vec{v} = \vec{v}_0 + \Delta \vec{v}$ 

#### Homework 3.14 Review



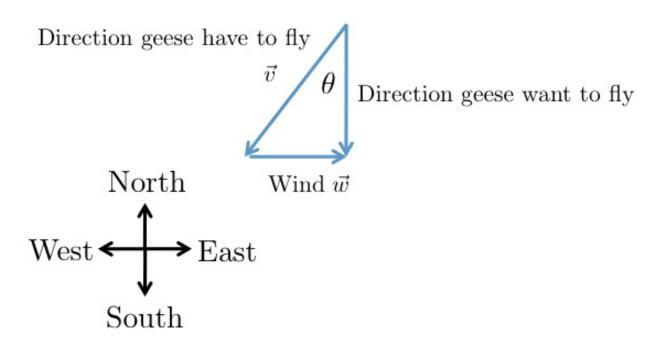
- Recommendations:
  - Always draw a picture: visual cues often help (like the direction of C here, since the problem states that C is such that

$$\vec{A} + \vec{B} + \vec{C} = 0$$

Practice trigonometry and the sohcahtoa mnemonic. Here

 $\sin \theta = \frac{\text{opposite}}{\text{hypoteneuse}} = \frac{B}{C} \quad \cos \theta = \frac{\text{adjacent}}{\text{hypoteneuse}} = \frac{A}{C} \quad \tan \theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{B}{A}$ • Know both vector components? Use the tangent! Vefferson Lab Prof. Satogata / Fall 2012 ODU University Physics 226N/231N 5

## Homework 3.29 Review



- The geese can fly 7.0 m/s relative to air (i.e. in still air)
  - But the wind is moving air, so part of their velocity needs to cancel out the wind speed
  - If the geese flew straight south, the wind on the side would push them off course.
  - Here again, the picture helps:
- $\sin\theta = \frac{w}{-}$

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